

What is An Effective Way to Quantify the Drug Safety Profile When Background Event Rates Are Low with An Application to Diabetes Cardiovascular Studies

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Lilly Diabetes Medical Affairs,
Global Patient Outcomes & Real World Evidence

May 19, 2015



- David Manner
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- 1 Introduction
- 2 Risk Ratio versus Risk Difference
- 3 Is Hazard Ratio A Good Measurement for Rare Events?
- 4 Restricted Mean Event Time Analysis
- 5 Diabetes CV Outcome Trials



Media

Press releases

2013

2012

2011

2010

2009

2008

2007

Fast facts

AstraZeneca announces initiation of two additional global studies with BRILINTA (ticagrelor)

Thursday, 14 November 2013

SOCRATES compares ticagrelor versus aspirin for the prevention of major vascular events in patients with acute ischemic stroke or transient ischemic attack

THEMIS compares ticagrelor versus placebo for the long-term prevention of major vascular events in patients with Type 2 diabetes at high cardiovascular risk

AstraZeneca today announced plans to conduct two new [clinical studies](#) as part of PARTHENON, AstraZeneca's largest clinical trial program involving over 80,000 patients. The studies are designed to build scientific understanding of BRILINTA® (ticagrelor) tablets in additional high-risk patient populations.

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http://www.astrazeneca-us.com/media/press-releases/Article/20131114-astrazeneca-announces-initiation-of-two-additional

	n	Intervention	Population	Primary outcome	Study status	Start and estimated end date	ClinicalTrials.gov identifier
TECOS	14 000	Sitagliptin versus placebo	T2DM; HbA _{1c} 6.5-8.0%; ≥50 years; CVD history	CV death, MI, UA, or stroke	Ongoing, not recruiting	12/2008-Q3/2014	NCT00790205
TOSCA IT	3371	Pioglitazone versus sulfonylurea	T2DM; HbA _{1c} ≥7.0% and ≤9.0%; metformin monotherapy	Death, MI, stroke or coronary revascularisation	Recruiting	09/2008-12/2018	NCT00700856
CANVAS	4330	Canagliflozin 100 mg versus canagliflozin 300 mg versus placebo	T2DM; ≥30 years; HbA _{1c} 7.0-10.5%; History of/high risk of CVD	CV death, MI, UA, or stroke	Ongoing, not recruiting	12/2009-03/2017	NCT01032629
ELIXA	6000	Lixisenatide versus placebo	T2DM; HbA _{1c} 5.5-11.0%; ACS	CV death, MI, UA, or stroke	Ongoing, not recruiting	06/2010-01/2015	NCT01147250
EXSCEL	14 000	Exenatide once weekly versus placebo	T2DM; HbA _{1c} 6.5-10.0%; CVD in about 60%	CV death, MI, or stroke	Recruiting	06/2010-12/2017	NCT01144338
BI 10773 trial	7000	Empagliflozin 10 mg versus empagliflozin 25 mg versus placebo	T2DM; ≥18 years; HbA _{1c} 7.0-10.0%; (7.0-9.0% drug naive); high CV risk	CV death, MI, or stroke	Ongoing, not recruiting	07/2010-03/2018	NCT01131676
LEADER	9340	Liraglutide versus placebo	T2DM; HbA _{1c} ≥7.0%; ≥50 years+CVD; ≥60 years+CV risk factors	CV death, MI, or stroke	Ongoing, not recruiting	08/2010-10/2015	NCT01179048
CAROLINA	6000	Linagliptin versus glimepiride	T2DM; HbA _{1c} 6.5-8.5%; 40-85 years; CVD/CV risk factors/diabetes end organ damage	CV death, MI, UA, or stroke	Ongoing, not recruiting	10/2010-09/2018	NCT01243424
REWIND	9622	Dulaglutide versus placebo	T2DM; HbA _{1c} ≤9.5%; 50 years+CVD; 55 years+subclinical CVD; ≥60 years+CV risk factors	CV death, MI, or stroke	Ongoing, not recruiting	07/2011-04/2019	NCT01394952
MK-3102 trial	4000	MK-3102 versus placebo	T2DM; CVD history	CV death, MI, UA, or stroke	Recruiting	10/2012-10/2017	NCT01703208
SUSTAIN6	3260	Semaglutide 0.5 mg versus semaglutide 1.0 mg versus placebo	T2DM; HbA _{1c} ≥7.0%; age ≥50 years+CVD; age ≥60 years+subclinical CVD	CV death, MI, or stroke	Ongoing, not recruiting	02/2013-01/2016	NCT01720446
ITCA650 trial	2000	ITCA 650 (exenatide in DUROS) versus placebo	T2DM; HbA _{1c} >6.5%; CVD history	CV death, MI, UA, or stroke	Recruiting	03/2013-07/2018	NCT01455896
DECLARE-TIMI 58	17 150	Dapagliflozin 10 mg versus placebo	T2DM; ≥40 years; high CV risk	CV death, MI, or stroke	Recruiting	04/2013-04/2019	NCT01730534
CARMELINA	8300	Linagliptin versus placebo	T2DM; HbA _{1c} 6.5-10%; 18 years; microalbuminuria or macroalbuminuria and previous macrovascular disease; impaired renal function with predefined UACR	CV death, MI, UA, or stroke	Recruiting	07/2013-01/2018	NCT01897532
DEVOTE	7500	Insulin degludec versus insulin glargine	T2DM; HbA _{1c} ≥7.0%; or HbA _{1c} ≤7.0% and insulin treatment; ≥50 years and CV or renal disease or ≥60 years and CV risk factors	CV death, MI or stroke	Recruiting	10/2013-11/2018	NCT01959529
Ertugliflozin trial	3900	Ertugliflozin 5 mg versus ertugliflozin 15 mg versus placebo	T2DM; HbA _{1c} 7.0-10.5%; CVD history	CV death, MI, or stroke	Recruiting	11/2013-06/2020	NCT01986881

T2DM= type 2 diabetes. CVD=cardiovascular disease. CV=cardiovascular. MI=myocardial infarction. UA=unstable angina. ACS=acute coronary syndrome.

Table 2: Ongoing cardiovascular outcome trials of glucose-lowering drugs or strategies (in order of starting date)

- Is it ethical to enroll so many patients in these studies? What if the drug is not safe?
- It takes so long to complete. Do we feel that the public would like to know the results quicker if the drug is not safe?
- How can we control operation bias for such large trials?
- Does the high cost of such trials become a barrier for drug companies to develop new treatments for patients?
- Do we have alternatives ...

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- The risk ratio (R) is $(5/100)/(4/100) = 5/4 = 1.25$ with 95% exact confidence interval as $(0.3352, 4.8164)$.
- It is worth to notice that the sample size 100 is not very useful when we calculate the risk ratio.

- In a two arm, randomized control trial, for treatment arm A, we observed 5 adverse events out of 1000 patients, and for treatment B, we observed 4 adverse events out of another 1000 patients.
- It is easy to see that the event proportions for treatment A is 5/1000, and for treatment B is 4/1000.
- The risk difference (D) is $5/1000 - 4/1000 = 1/1000$ (i.e. 0.1%) with 95% exact confidence interval as (-0.6984%, 0.8505%).
- The risk ratio (R) is $(5/1000)/(4/1000) = 5/4 = 1.25$ with 95% exact confidence interval as (0.3240, 4.9863).
- The confidence interval for risk difference shrinks a lot but the confidence interval for risk ratio is virtually unchanged.

Lilly What did we see here?

Sample size	Trt A	Trt B	D	R
100	5	4	1/100	5/4
1000	5	4	1/1000	5/4
10000	5	4	1/10000	5/4

Lilly What did we see here?

Sample size	Trt A	Trt B	D	R
100	5	4	1/100	5/4
1000	5	4	1/1000	5/4
10000	5	4	1/10000	5/4

- As sample size increases, the risk difference becomes smaller and smaller, but the risk ratio is unchanged.
- The risk ratio calculation ignore the sample size which makes useful information unused.
- For rare events, due to variability, the risk ratio estimation is not stable.
- When lacking the background rate information, the risk ratio may be misleading. From 50% to 60% is 20% risk increase, and it is the same amount of increase from 1% is 1.2%.

Frequentist point of view

From frequentist point, we would like to estimate a parameter, and a good estimate should have a smaller variance which can provide more accurate estimate to what we would like to know. We show that risk difference can be estimated more accurately.

Bayesian point of view

From Bayesian perspective, we compare the difference between prior and posterior distributions updated by the observed data. A measurement contained more information will update the prior more. We show that under a reasonable non-informative prior, risk difference contains more information (because it takes sample size into account!)

If you believe in these two points, you can skip some technical details by

▶ [click here!](#)

Frequentist

$$\hat{D} \sim N \left\{ D, \frac{p_1(1-p_1) + p_2(1-p_2)}{n} \right\},$$
$$\hat{R} \sim N \left\{ R, \frac{p_1^2 + p_2^2 - p_1 p_2 (p_1 + p_2)}{np_2^3} \right\}.$$

It is easy to see that if $p_1 \approx p_2 = p$, the variance of \hat{D} goes to zero with a rate about p/n , but the variance of \hat{R} goes to zero with a rate about $1/(np)$. It is obvious that when p is small, \hat{D} can more quickly converge to the truth than \hat{R} . In particular, the ratio of the variance is $V(\hat{D})/V(\hat{R}) = p^2 + o(p^2)$.

Bayesian

For a probability density function $f(x)$, the entropy is defined as,

$$\begin{aligned}h(f) &= - \int f(x) \log\{f(x)\} dx \\ &= \log(u) - \int f(x) \log \frac{f(x)}{1/u} dx\end{aligned}$$

For a normal distribution, $h(f) = 1/2 \log(2\pi\sigma^2) + 1/2$. Since $V(\hat{D})/V(\hat{R}) = p^2 + o(p^2)$, \hat{D} contains more information than \hat{R} (higher entropy means less information). This also has a Bayesian interpretation that if we have a flat prior about D , say $U(-1, 1)$, and a flat prior about R as $U(0, u)$, $\log(u) - h(f)$ can be viewed as how much information we gain from a uniform prior (Kullback-Leibler Divergence). For rare event situation, when prior for R is between $(0, 200)$, the \hat{D} provides more information.

Lilly Kullback-Leibler divergence is invariant

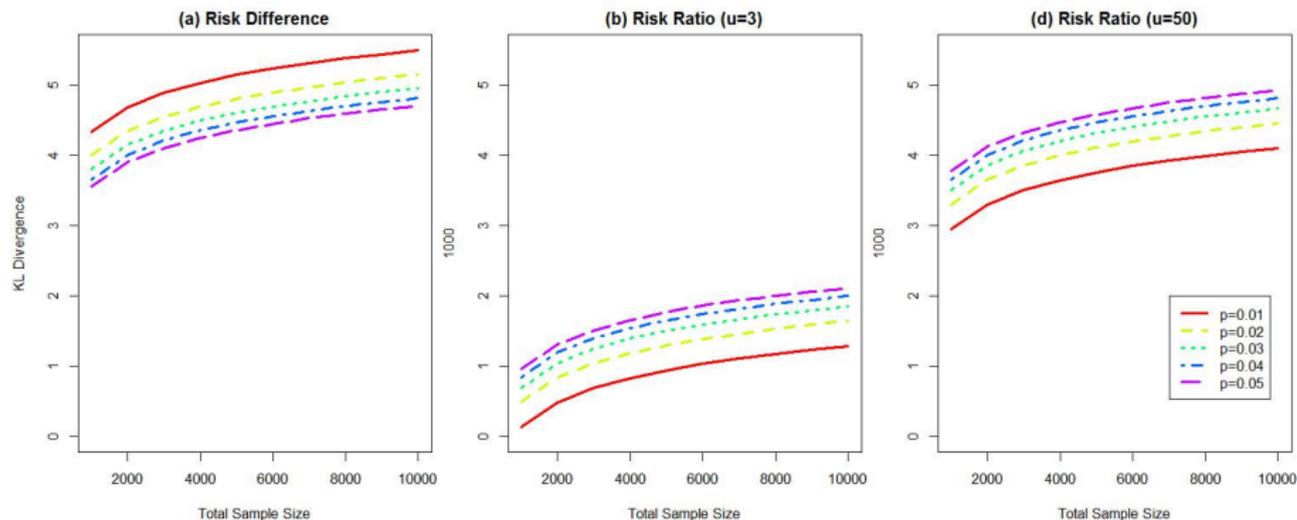
Let $f(x)$ and $g(x)$ be two density functions, and $x = h(y)$ be a transformation function with a non-vanishing Jacobian, i.e.

$|\partial h(y)/\partial y| \neq 0$. The new transformed density functions are, $f_Y(y) = f\{h(y)\}|\partial h(y)/\partial y|$ and $g_Y(y) = g\{h(y)\}|\partial h(y)/\partial y|$, respectively. So we have,

$$\begin{aligned}\int f(x) \log \frac{f(x)}{g(x)} dx &= \int f\{h(y)\}|\partial h(y)/\partial y| \cdot \log \frac{f\{h(y)\}}{g\{h(y)\}} dy \\ &= \int f\{h(y)\}|\partial h(y)/\partial y| \cdot \log \frac{f\{h(y)\}|\partial h(y)/\partial y|}{g\{h(y)\}|\partial h(y)/\partial y|} dy \\ &= \int f_Y(y) \log \frac{f_Y(y)}{g_Y(y)} dy.\end{aligned}$$

In particular, we have,

$$\begin{aligned}\log(u) - h(f) &= \int f(x) \log \frac{f(x)}{1/u} dx \\ &= \int af(ax + b) \log \frac{af(ax + b)}{a/u} dx.\end{aligned}$$



Conclusion: under reasonable priors, risk difference measured by a study with 1000 patients could be more informative than a 10,000 patients study measured by risk ratio.

For rare event situations, if we agree that risk difference contains more information, why we continue to provide risk ratios as less informative quantities to patients and public? We encourage people to think the change.

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- How does it apply to our diabetes CV outcome trials

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- Why hazard ratio can't capture this?! It is counter intuitive!
- The simple reason is that the hazard ratio can't take the sample size and duration of exposure into account!

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- No events situation can be translated to rare event cases in real trials.
- So, non-inferiority trial and superiority study might be different!

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- The proportional hazard assumption is a strong assumption (the hazard ratio is constant over time). When the proportion hazard(PH) assumption is violated...

- It is difficult to interpret which parameter we try to estimate; it is not an average of hazard ratio over time (Kalbfleisch and Prentice, 1981).
- The parameter estimated depends on censoring distributions !!
- Inference based on hazard ratio estimate (including the logrank test) are not efficient to detect the group difference.(Struthers and Kalbfleisch, 1986; Lin and Wei, 1989).

- Median failure time (may not be estimable).
- t-year survival rate (not an overall measure).
- Number needed to treat (NNT) or number needed to harm (NNH) (not an overall measure and unstable for rare events).
- Restricted Mean Event Time (RMET).
- There is a long history of using RMET for time to event analysis. (Irwin, 1949; Karrison, 1987; Zucker, 1998; Murray and Tsiatis, 1999; Chen and Tsiatis, 2001; Andersen et al., 2004; Zhang and Schaubel, 2011; Royston and Parmar, 2011; Zhao et al., 2012; Tian et al., 2013, 2014).

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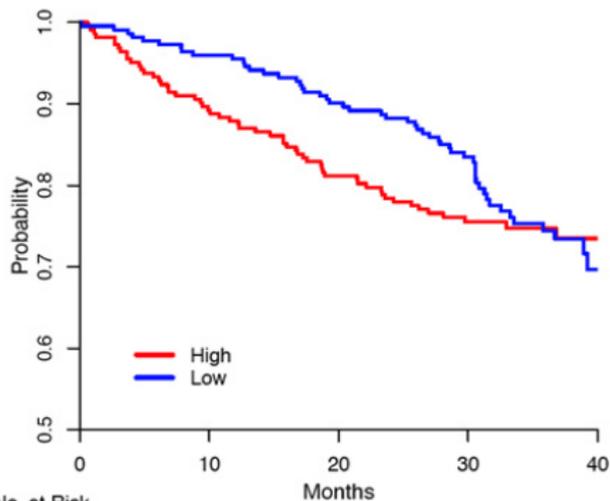
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- An example of using RMET. It illustrates how to use RMET and how to interpret the results.
- Estimation methods and inference methods.
- Simulation to demonstrate the estimation is accurate, and type I errors are well controlled.
- We apply it to diabetes CV outcome trials, and how it will impact the sample size.

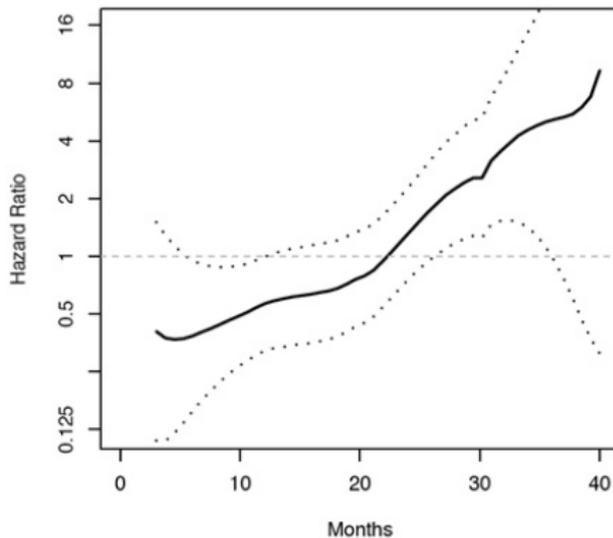
- E4A03 trial to compare low- and high-dose dexamethasone for patients with newly diagnosed multiple myeloma.
- One of the endpoints is overall survival $n = 445$.
- The trial stopped early at the second interim analysis; the low dose was superior.

A. Kaplan–Meier curves



No. at Risk					
High	223	199	179	122	20
Low	222	213	198	146	24

B. Ratio of hazards over time



- The proportional hazards assumption is not valid.
- The PH estimator is estimating a quantity which cannot be interpreted and, worse, depends on the study-specific censoring distributions.
- The logrank test is not powerful.
- In conventional analysis, we have Log-rank test: $p = 0.47$ and hazard ratio: $HR=0.87$ (0.60, 1.27).

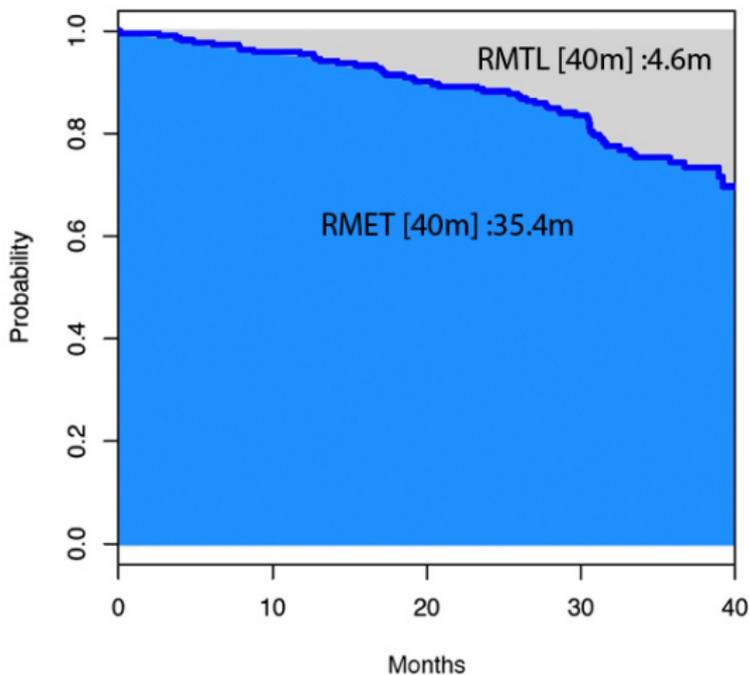


Figure: Kaplan-Meier curve for low dose arm. Restricted mean event time (RMET) and restricted mean time lost (RMTL)

- Restricted mean (up to 40 months).
- 35.4 months vs. 33.3 months.
- Difference = 2.1 (0.1, 4.2) months; $p = 0.04$.
- Ratio of RMET = $35.4/33.3 = 1.06$ (1.00, 1.13).
- Ratio of time lost = $6.7/4.6 = 1.46$ (1.02, 2.13).

Can we use this approach for diabetes cardiovascular outcome studies? For a 3 year CVOTs, the RMET for a patient is 1062.8 days. If we run such a trial, what is the acceptable non-inferiority margin?

- 106 days $\approx 1062.8 * 10\%$.
- 53 days $\approx 1062.8 * 5\%$.
- 26 days $\approx 1062.8 * 2.5\%$.

We are going to show you that we have good methods to accurately estimate RMET, and they can control type I errors very well. If you are already convinced and would like to see the diabetes CV trial simulation results, you can [▶ click here!](#)

- T_i : event time.
- C_i^d : dropout censoring time. C_i^a : administrative censoring time.
- $I(\cdot)$: indicator function.
- $C_i = C_i^d \wedge C_i^a$. $Y_i = T_i \wedge C_i$. $\Delta_i = I(T_i \leq C_i)$.
- X_i : a covariate vector.
- (Y_i, Δ_i, X_i) : observed data.
- τ : a time point where $P(Y_i > \tau) > 0$.
- $T_i^\tau = T_i \wedge \tau$: restricted event time.
- $Y_i^\tau = Y_i \wedge \tau$. $\Delta_i^\tau = I(T_i \wedge \tau \leq C_i)$.
- $(Y_i^\tau, \Delta_i^\tau, X_i)$: derived data based on τ .

RMET definition

$$\mu^\tau(X) = E(T_i^\tau | X) = \int_0^\tau S(t|X) dt, \quad (1)$$

where $S(t)$ is the survival function.

Estimation

$$\tilde{\mu}^\tau = \int_0^\tau \hat{S}(t) dt,$$

where \hat{S} is a Kaplan-Meier (KM) estimator for the survival function of T based on $\{(Y_i, \Delta_i), i = 1, \dots, n\}$.

Based on the martingale approach from Andersen (1993), we have,

Variance estimator of $\tilde{\mu}^\tau$ (area under the KM curve)

Let $t_1 < t_2 < \dots < t_D$ are the unique events time, and d_i is the number of events at t_i . We have,

$$\hat{V}(\tilde{\mu}^\tau) = \sum_{i=1}^D \left\{ \int_{t_i}^{\tau} \hat{S}(t) dt \right\}^2 \frac{d_i}{R(t_i)\{R(t_i) - d_i\}}, \quad (2)$$

where $R(t) = \sum_{i=1}^n I(Y_i \geq t)$.

Therefore, based on (Klein and Moeschberger, 2003), the confidence interval can be constructed as,

$$\tilde{\mu}^\tau \pm Z_{1-\alpha/2} \sqrt{\hat{V}(\tilde{\mu}^\tau)}.$$

Logic review

$$\mu^T(X) \stackrel{?}{=} \beta^T X.$$

$$\Downarrow$$

$$\eta\{\mu^T(X)\} = \beta^T X.$$

$$\Downarrow$$

Estimating equation

$$\Downarrow$$

IPW estimate.

Now, we start from IPW estimate, then show the link function with estimating equation in the next a few slides ...

Estimation

$$\hat{\mu}^\tau = n^{-1} \sum_{i=1}^n \frac{\Delta_i^\tau}{\hat{G}(Y_i^\tau)} Y_i^\tau, \quad (3)$$

where $\hat{G}(\cdot)$ is the KM estimator of the censoring time C based on $\{(Y_i, 1 - \Delta_i), i = 1, \dots, n\}$.

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Key message

$\hat{\mu}$ and $\tilde{\mu}$ are asymptotically equivalent at the $n^{-1/2}$ rate.

Based on the results from Satten and Datta (2001), we have,

$$\begin{aligned} \hat{S}(t) &= 1 - \int_0^t \hat{S}(u^-) \frac{dN(u)}{R(u)} = 1 - \frac{1}{n} \int_0^t \frac{dN(u)}{\hat{G}(u^-)} + O_p(n^{-1/2}) \\ &= 1 - \frac{1}{n} \sum_{i=1}^n \frac{I(Y_i \leq t) \Delta_i^\tau}{\hat{G}(Y_i)} + O_p(n^{-1/2}) \\ &= \frac{1}{n} \sum_{i=1}^n \frac{I(Y_i > t) \Delta_i^\tau}{\hat{G}(Y_i)} + O_p(n^{-1/2}) \end{aligned}$$

where $N(t) = \sum_{i=1}^n I(Y_i \leq t) \Delta_i$, $R(t) = \sum_{i=1}^n I(Y_i \geq t)$, and $\hat{\Lambda}(\cdot)$ is the Nelson-Aalen estimator of the cumulative hazard function of T . Therefore,

$$\hat{\mu}^\tau - \tilde{\mu}^\tau = \hat{\mu}^\tau - \frac{1}{n} \sum_{i=1}^n \int_0^\tau \frac{I(Y_i > t) \Delta_i^\tau}{\hat{G}(Y_i)} dt + O_p(n^{-1/2}) = O_p(n^{-1/2}). \quad \square$$

Modified logic link

$$\begin{aligned}\eta\{\mu^\tau(X)\} &= \log \frac{\mu^\tau(X)}{\tau - \mu^\tau(X)} \\ &= \beta^T X.\end{aligned}$$

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Here, the regression coefficient of the treatment indicator is,

$$\log \left[\frac{\mu^\tau(X^t) \cdot \{\tau - \mu^\tau(X^c)\}}{\mu^\tau(X^c) \cdot \{\tau - \mu^\tau(X^t)\}} \right],$$

which is an odds ratio to summarize the treatment difference.

Estimating equation

$$S_n(\beta) = \sum_{i=1}^n \frac{\Delta_i^\tau}{\hat{G}(Y_i^\tau)} X_i \{Y_i^\tau - \eta^{-1}(\beta^\tau X_i)\}. \quad (4)$$

Let β_0 be the true parameter and we estimate β_0 by solving the estimating equation $S_n(\beta) = 0$. Under mild conditions, $n^{-1}S_n(\beta_0) \xrightarrow{\mathcal{P}} 0$. So the estimate $\hat{\beta}$ is consistent.

- 1 Calculate \hat{B} : Let $\hat{\xi}_i = \frac{\Delta_i^\tau}{\hat{G}(Y_i^\tau)} X_i \{ Y_i^\tau - \eta^{-1}(\hat{\beta}^\tau X_i) \}$, and we have
$$\hat{B} = n^{-1} \sum_{i=1}^n \hat{\xi}_i \hat{\xi}_i^\tau.$$
- 2 Generate ω_j : $\omega_j \sim N(0, \hat{B}^{-1})$, $i = 1, \dots, M$.
- 3 Evaluate ψ_j . $\psi_j = n^{-1/2} S_n(\hat{\beta} + n^{-1/2} \omega_j)$.
- 4 Estimate Σ : $\hat{\Sigma}^{-1} = M^{-1} \sum_{j=1}^M \psi_j \psi_j^\tau$.

- 1 Calculate \hat{B} : Let $\hat{\xi}_i = \frac{\Delta_i^T}{\hat{G}(Y_i^T)} X_i \{ Y_i^T - \eta^{-1}(\hat{\beta}^T X_i) \}$, and we have
$$\hat{B} = n^{-1} \sum_{i=1}^n \hat{\xi}_i \hat{\xi}_i^T.$$
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- 4 Estimate Σ : $\hat{\Sigma}^{-1} = M^{-1} \sum_{j=1}^M \psi_j \psi_j^T$.

A magic!

$$n^{1/2}(\hat{\beta} - \beta_0) \xrightarrow{\mathcal{D}} N\{0, \Sigma\}$$

Because, we have the following expansion,

$$n^{-1/2} S_n(\beta) = A n^{1/2}(\beta - \beta_0) + n^{-1/2} \sum_{i=1}^n \xi_i + o_p(1 + n^{1/2} \|\beta - \beta_0\|).$$

Simulation model

$$\eta\{\mu^T(X)\} = a_0 + a_1 \text{Trt} + a_2 U,$$

where Trt is treatment with value equal to 0 or 1, and U is a uniform distribution with support $(0, 1)$.

Simulation studies include,

- Estimation of the parameters.
- The confidence interval coverage.
- Power and type I error control.
- Sample size calculation for Diabetes CVOTs.

- True value $a_0 = -2.5$, $a_1 = 1$, and $a_2 = 1$.
- Constant hazard for events, uniform censoring time. Can you figure out how we simulate event times? :)
- $\tau = 24$.
- 500 patients per arm. 1000 simulation runs.
- Estimation results in mean(sd): $-2.499(0.107)$, $0.999(0.088)$, and $0.999(0.173)$.
- 95% confidence interval coverage: $(0.949, 0.955, 0.952)$.

Conclusion: the estimation is robust and accurate in these simulation settings.

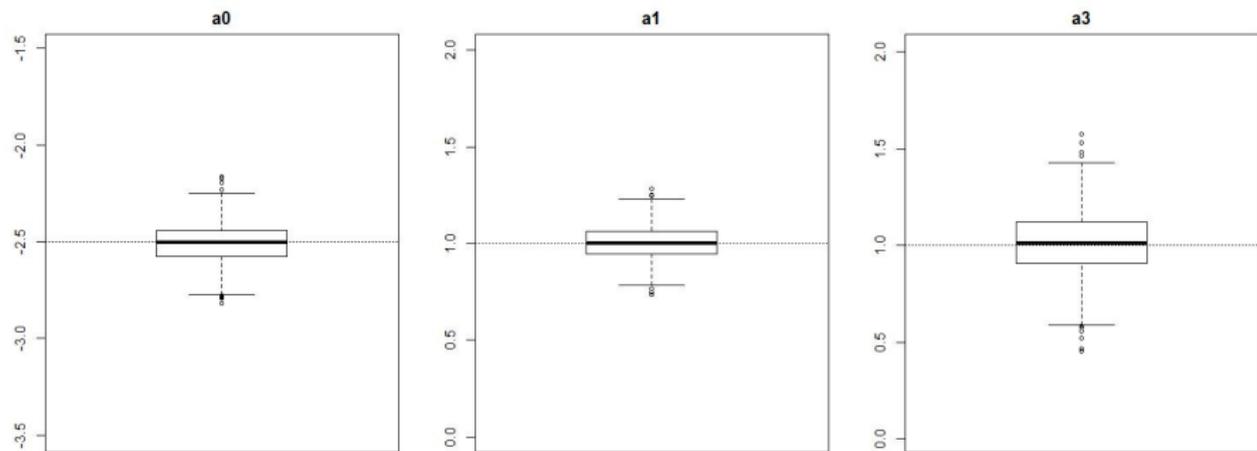


Figure: Boxplots of the estimates

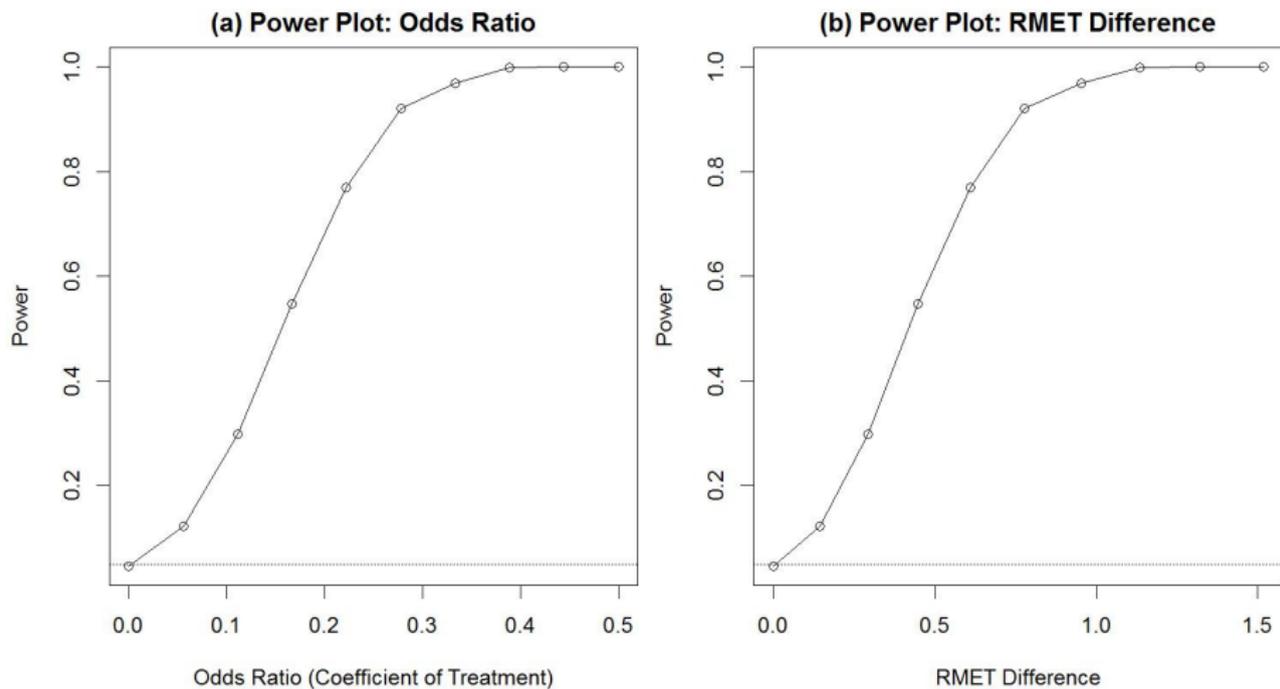
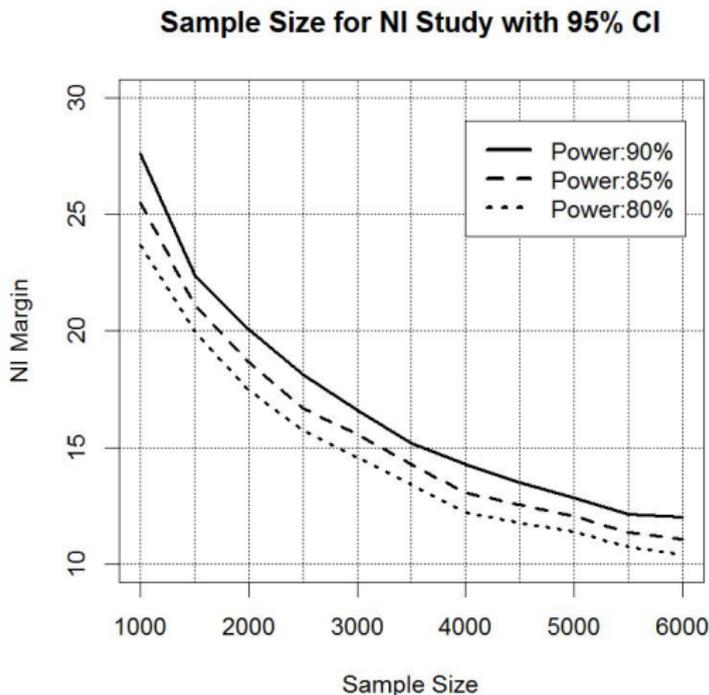


Figure: Type I error control and power plots

- Annual event rate is 2%.
- Annual dropout rate is 1%.
- Study period for each patient is 36 months.
- RMET is for 36 months.
- Non-inferiority study assumes both arm has the same event rate.
- Non-inferiority margin is based on 95% confidence interval.
- The event rate and dropout rate assumption are translated to 1062.8 days RMET for this patient population.



Example: If we choose the non-inferiority margin as 20 days, 2000 patients will provide 90% power.

- We must pre-define the time period for which the RMET will be calculated.
- How we can choose the patients from standard care patients? this would prevent someone choosing a very low CV risk population- prevent “gaming the design” .
- We need to pre-define non-inferiority margin in days. So that we have to gain clinical consensus on what is a meaningful difference in days.

Notes: by the assumption, 3 year event rate is 5.75%. With 2000 patients, we expect to observe 114.9 events with standard deviation equal to 10.4. A 95% confidence interval for the observed 3 year event rate is [4.72%,6.76%].

- There are 3 major limitations of using hazard ratio and proportion hazard models
 - It can't well take duration of exposure and sample size into consideration.
 - Superiority studies and non-inferiority studies might be different.
 - There are many issues when proportional hazard assumption is not valid.
- RMET is a good alternative.
- Through the estimation and inference methods for RMET is robust. In particular, our proposed method can well control the type I error rate.
- When it is appropriately used, it has a great potential to significantly reduce the sample size for diabetes CVOTs.
- We need to work together to change the paradigm including influencing regulatory agents.
- There are strong support from external thought leaders.
- We believe that there is great opportunities to shift the paradigm which is eventually good for the patients.

I believe that
*every complex problem has a simple, neat
and elegant solution ...*

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